

Workshop Goals



Participants will understand:

- The components and structure of Bridges Intervention volumes
- The research behind Bridges Intervention's development
- The role of questioning, visualization, wait time, and the eight Mathematical Practices in implementation
- The use of placement assessments, progress monitoring tools, and scoring guides

Fluency with the Number Rack & Math Practices

Live Session 2

Why Visual Models?



“The different evidence that is coming from the neuroscientists tells us that our brain wants to think visually about maths. Building students’ mathematical understanding doesn’t just mean strengthening one area of the brain that is involved with abstract numbers, it means strengthening connections between areas of the brain and strengthening the visual pathways.”

– Jo Boaler, youcubed.org

Number Frames



Five-frame

Bundles & Sticks...to Tally Marks

Number Frames



Five-frame



Ten-frame

Bundles & Sticks...to Tally Marks

Number Frames



Five-frame



Ten-frame



Double ten-frame

Bundles & Sticks...to Tally Marks

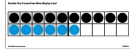
Number Frames



Five-frame



Ten-frame



Double ten-frame

Bundles & Sticks...to Tally Marks



Craft sticks showing 7 as tallies

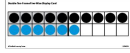
Number Frames



Five-frame



Ten-frame



Double ten-frame

Bundles & Sticks...to Tally Marks



Craft sticks showing 7 as tallies



A bundle of 10 and 3 more makes 13

Number Frames



Five-frame



Ten-frame



Double ten-frame

Bundles & Sticks...to Tally Marks



Craft sticks showing 7 as tallies



A bundle of 10 and 3 more makes 13

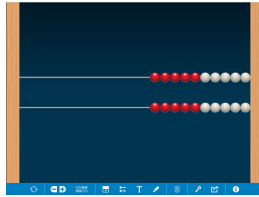


Tally marks showing 8

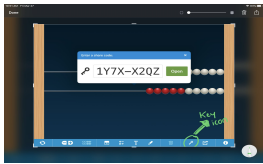
Let's Explore the Number Rack



What do you notice about this model?



Problem-Solving on the Number Rack



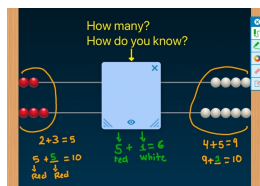
Click the key icon on the lower right and input the code in the picture.

Strengthening Connections

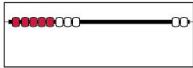


How does this example support:

- verbal
- quantitative
- symbolic

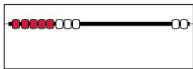


Number Racks

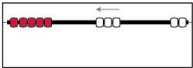


"1, 2, 3, 4, 5, 6, 7, 8.
That's 8."

Number Racks

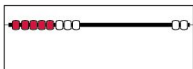


"1, 2, 3, 4, 5, 6, 7, 8.
That's 8."

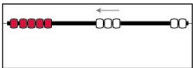


"First slide 5, and then
3 more makes 8."

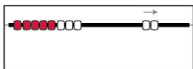
Number Racks



"1, 2, 3, 4, 5, 6, 7, 8.
That's 8."



"First slide 5, and then
3 more makes 8."



"I know it's 8 because
it's 2 less than 10."

Where Are the Math Practices?



Habits of Mind of a Productive Mathematical Thinker

MP.1 Make sense of problems and persevere in solving them.
MP.6 Attend to precision.

Reasoning and Explaining

MP.2 Reason abstractly and quantitatively.
MP.3 Construct viable arguments and critique the reasoning of others.

Modeling and Using Tools

MP.4 Model with mathematics.
MP.5 Use appropriate tools strategically.

Seeing Structure and Generalizing

MP.7 Look for and make use of structure.
MP.8 Look for and express regularity in repeated reasoning.

Using the Number Rack



Where Are the Math Practices?



Habits of Mind of a Productive Mathematical Thinker

MP.1 Make sense of problems and persevere in solving them.
MP.6 Attend to precision.

Reasoning and Explaining

MP.2 Reason abstractly and quantitatively.
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Modeling and Using Tools

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Seeing Structure and Generalizing

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Ten-Minute Break



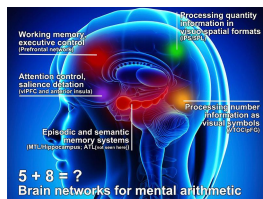
Multiplication & Division Arrays

Live Session 3

Jo Boaler's Research – Visual Mathematics

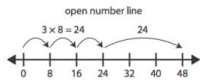
Our brains are made up of 'distributed networks,' and when we handle knowledge, different areas of the brain light up and communicate with each other. [...]

Neuroimaging has shown that even when people work on a number calculation, such as 12×25 , with symbolic digits (12 and 25) our mathematical thinking is grounded in visual processing.



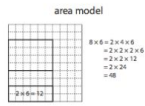
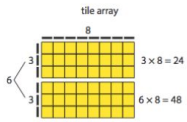
From Seeing As Understanding: The Importance of Visual Mathematics for Our Brain and Learning by Jo Boaler, Professor of Mathematics Education, with Ling Chen, Stanford Cognitive and Systems Neuroscience Lab, Cathy Williams & Montserrat Cordero, youcubed (interviewed from youcubed.org)

Visual Math = Accessible Math Instruction 

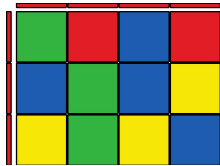


ratio tables

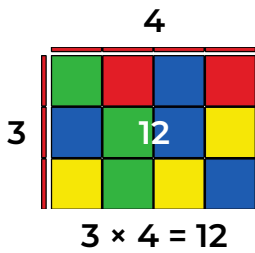
Rows of crayons	Number of crayons
1	8
2	16
3	24
$\times 2 \rightarrow 6$	$48 \rightarrow \times 2$



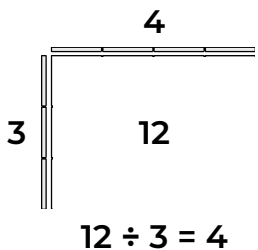
Dimensions & Area 



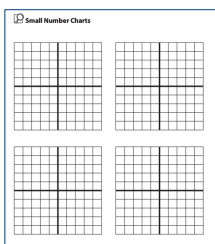
Dimensions & Area 



Dimensions & Area



Representational with Grid Paper



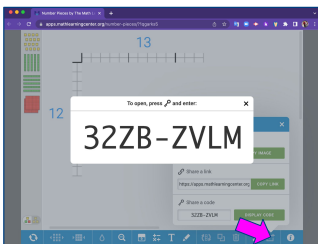
Array Model Video



Base Ten Pieces



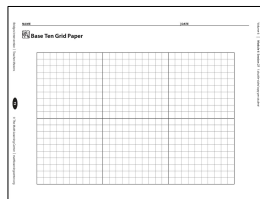
Base Ten Pieces



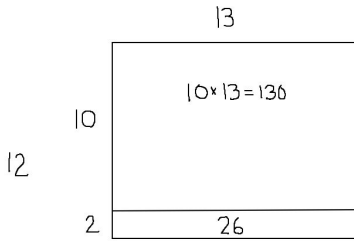
Using Grid Paper

Concrete → Representational → Abstract

What would 12x13 look like using grid paper?



Sketching Arrays



$$\begin{array}{r} 13 \\ \times 12 \\ \hline 26 \\ + 130 \\ \hline 156 \end{array}$$

Placement Assessment & Entry Points

Volume Placement Assessment



1. Read directions for administering the Volume Placement Assessment.

- What did you learn?
- What Visual Models will students use?
- During which part of the assessment will they use these tools?

Placement Assessment & Scoring Guide

- **Read through the Placement Assessment with your students in mind.**
 - What concepts and skills are being assessed?
 - How does this Placement Assessment progress from Part 1 to Part 2 to Part 3?
- **Read through the scoring guide.**
- **Think about and discuss how the scoring guide helps determine a starting point.**

Placement Assessment Volume 6

- **Examine the student work.**
 - What does the student understand?
- **With a partner, score the student work using the scoring guide.**
 - What do you notice?
 - What do you wonder?
 - Where would you begin?
- **Debrief**

Entry Points

- Give students the gift of time with the models and strategies in Unit 1 and Sept. Number Corner.
- Use the support suggestions in the Bridges sessions, Work Places & Number Corner.
- Gather data from:
 - **Teacher recommendations**
 - **Unit Post-Assessments & Number Corner Checkups**
 - **Bridges Intervention Placement Assessments as needed**
- Be flexible! Work between volumes.
- By grade, by standard?

Entry Points



- Give students the gift of time with the models and strategies in Unit 1 of your core curriculum.
- Gather data from:
 - Teacher recommendations
 - Unit Post-Assessments
 - District Assessments such as STAR or MAP
 - Bridges Intervention Placement Assessments as needed
- Be flexible! Work between volumes.
- By grade, by standard?

Instructional Targets



Starting Points provides information about modules and suggested starting places based on specific grade-level standards and expectations.

Grade	Major Instructional Targets	Recommended Instructional Design for Bridges Intervention
1	1.OA.A Addition Fluency 1.OA.A.1 Fluently add and subtract within 20 using a variety of strategies. 1.OA.A.2 Understand the meaning of the plus sign (+) and the minus sign (-). 1.OA.A.3 Apply addition and subtraction within 20 to solve word problems involving unknowns in all positions. 1.OA.A.4 Represent addition and subtraction problems with a drawing or equation.	Unit 1 (Modules 1-4) Unit 2 (Modules 5-8) Unit 3 (Modules 9-12)
2	2.OA.A Addition Fluency 2.OA.A.1 Fluently add and subtract within 20 using mental strategies. 2.OA.A.2 Understand the meaning of the plus sign (+) and the minus sign (-). 2.OA.A.3 Apply addition and subtraction within 20 to solve word problems involving unknowns in all positions. 2.OA.A.4 Represent addition and subtraction problems with a drawing or equation.	Unit 1 (Modules 1-4) Unit 2 (Modules 5-8) Unit 3 (Modules 9-12)
3	3.OA.A Multiplication Fluency 3.OA.A.1 Use multiplication to solve word problems involving unknowns in all positions. 3.OA.A.2 Understand the meaning of the multiplication sign (×). 3.OA.A.3 Apply multiplication within 100 to solve word problems involving unknowns in all positions. 3.OA.A.4 Represent multiplication problems with a drawing or equation.	Unit 1 (Modules 1-4) Unit 2 (Modules 5-8) Unit 3 (Modules 9-12)

Working by Standard



Grade 1	Volume 1	Volume 2	Volume 3	Volume 4
1.OA.1 Solve addition and subtraction story problems within 20.				Modules 1-4
1.OA.3 Count on/cross back to add & subtract.	Modules 4-6	Modules 2, 3		Modules 3-5
1.OA.4 Add & subtract within 20 using strategies and properties.	Modules 4-6	Module 2, Module 3		Modules 3-6
1.OA.8 Understand that the equal sign indicates equivalence.		Modules 5-7		
1.OA.8 Solve for the unknown in an addition or subtraction equation.	Module 6	Modules 1-3, 5-6		Modules 3-6
1.NBT.1 Count to 120, starting at any number less than 120.	Modules 4-6			
1.NBT.3 Read & write numerals to 120.	Modules 4-6		Modules 1, 3	
1.NBT.2 Understand 2-digit place value.	Module 3		Modules 1, 2	
1.NBT.3 Compare 2-digit numbers; record the results with =, <, and >.	Module 3		Module 1	
1.NBT.4 Add within 100.	Module 3		Modules 2, 3	
1.NBT.5 Identify first 10 names or 10 less than a 3-digit number.				Modules 1, 2

Set 1 or Set 2 Overview, Section 2: Navigating the Resources

Reflections

Reflecting on the Goals



Participants will understand:

- The components and structure of Bridges Intervention volumes
- The research behind Bridges Intervention's development
- The role of questioning, visualization, wait time, and the eight Mathematical Practices in implementation
- The use of placement assessments, progress monitoring tools, and scoring guides

Reflection



What is one thing you learned during the workshop or one thing that was meaningful or important?

MLC Support

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